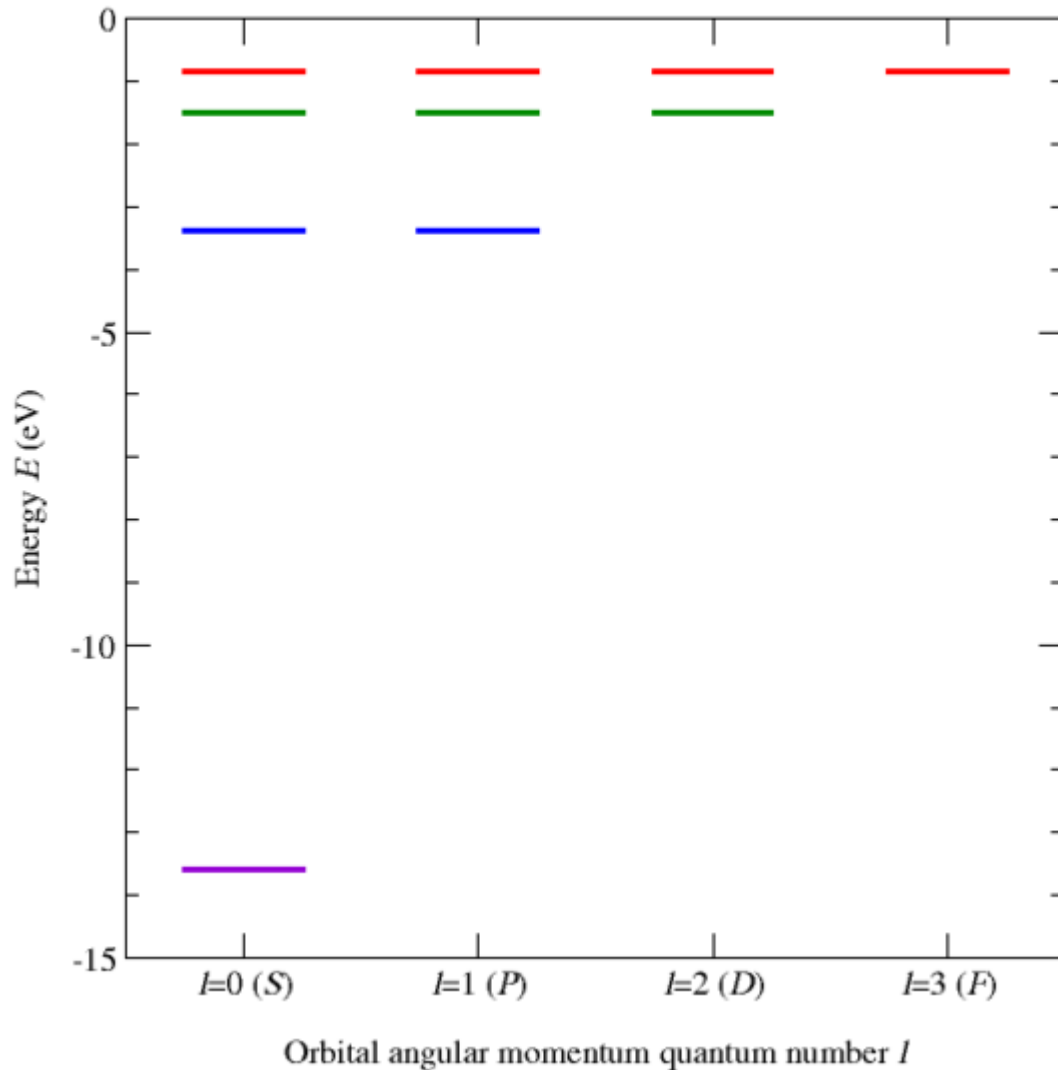




# Basic Energy Levels

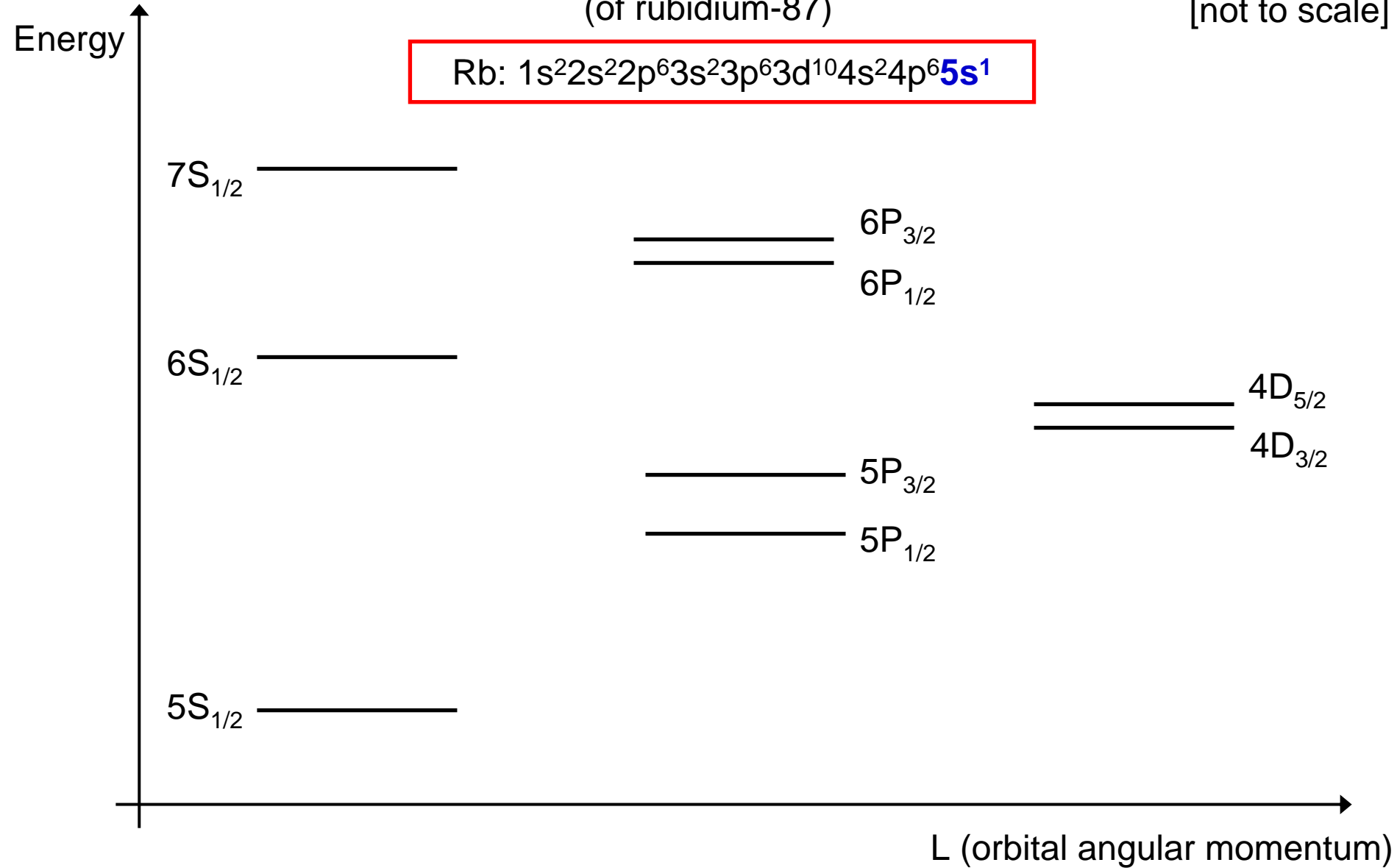
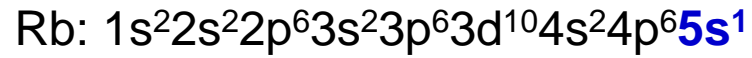
Energy Levels of Hydrogen ( $n=1-4$ )



# Fine Structure

(of rubidium-87)

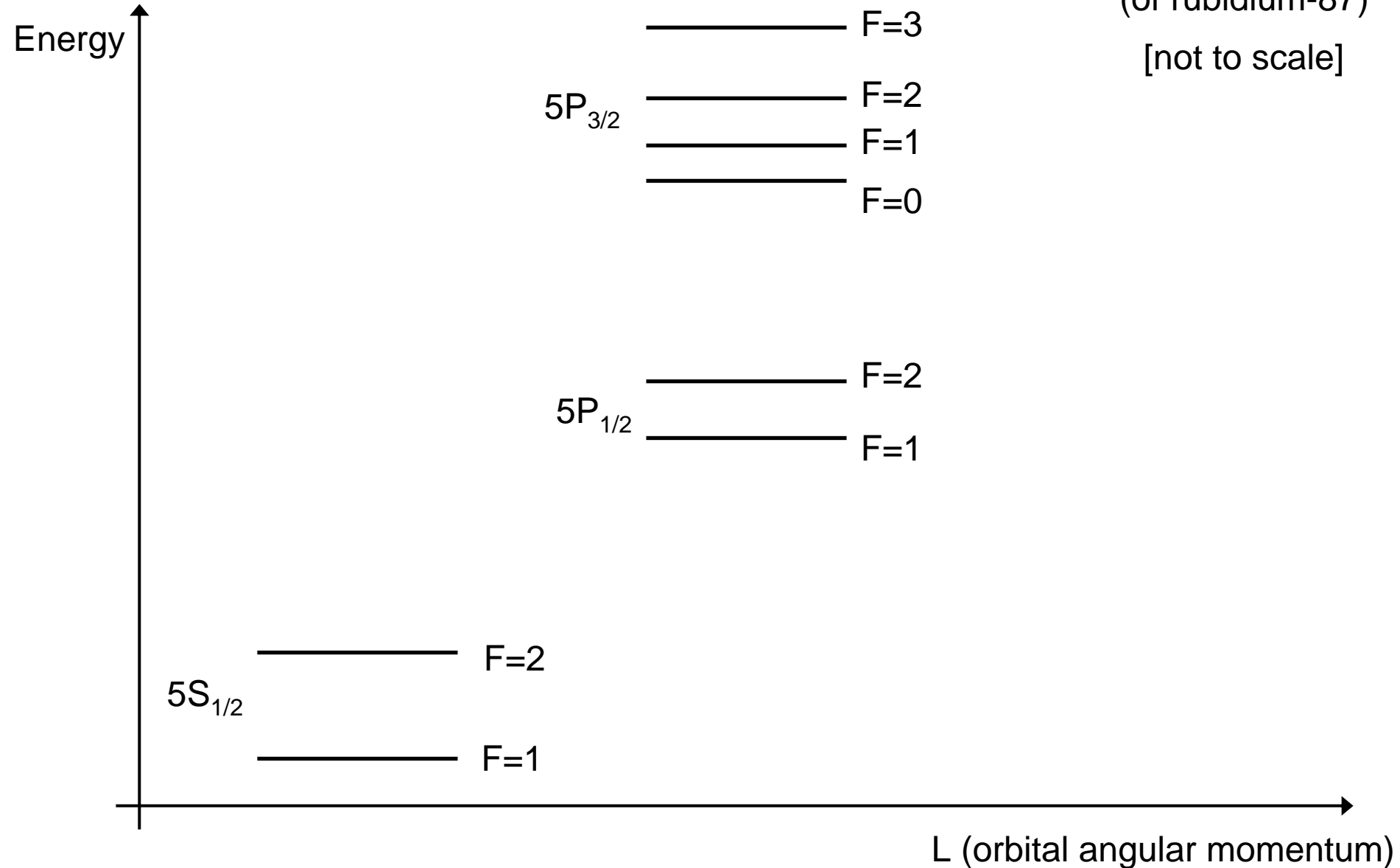
[not to scale]



# Hyperfine Structure

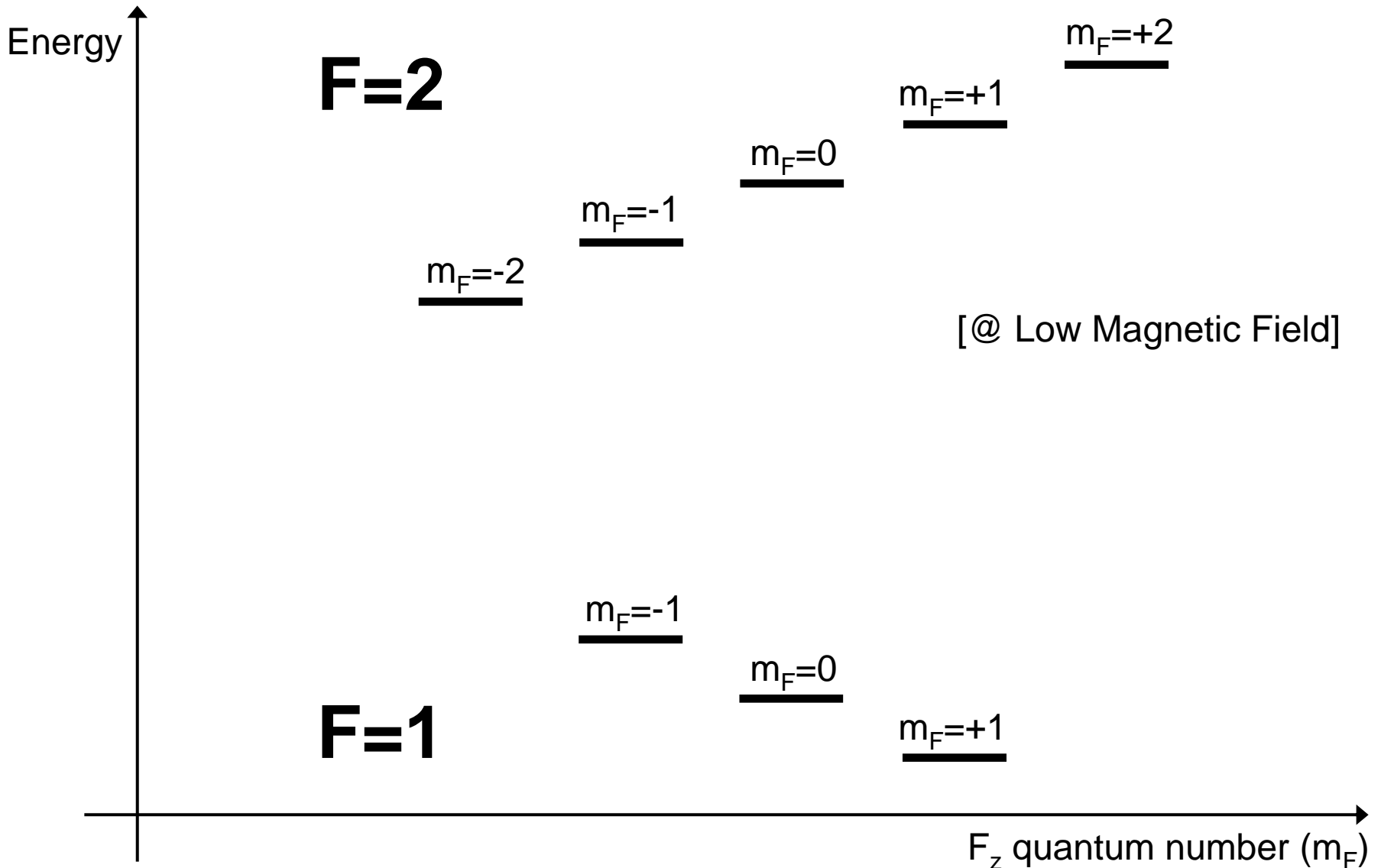
(of rubidium-87)

[not to scale]

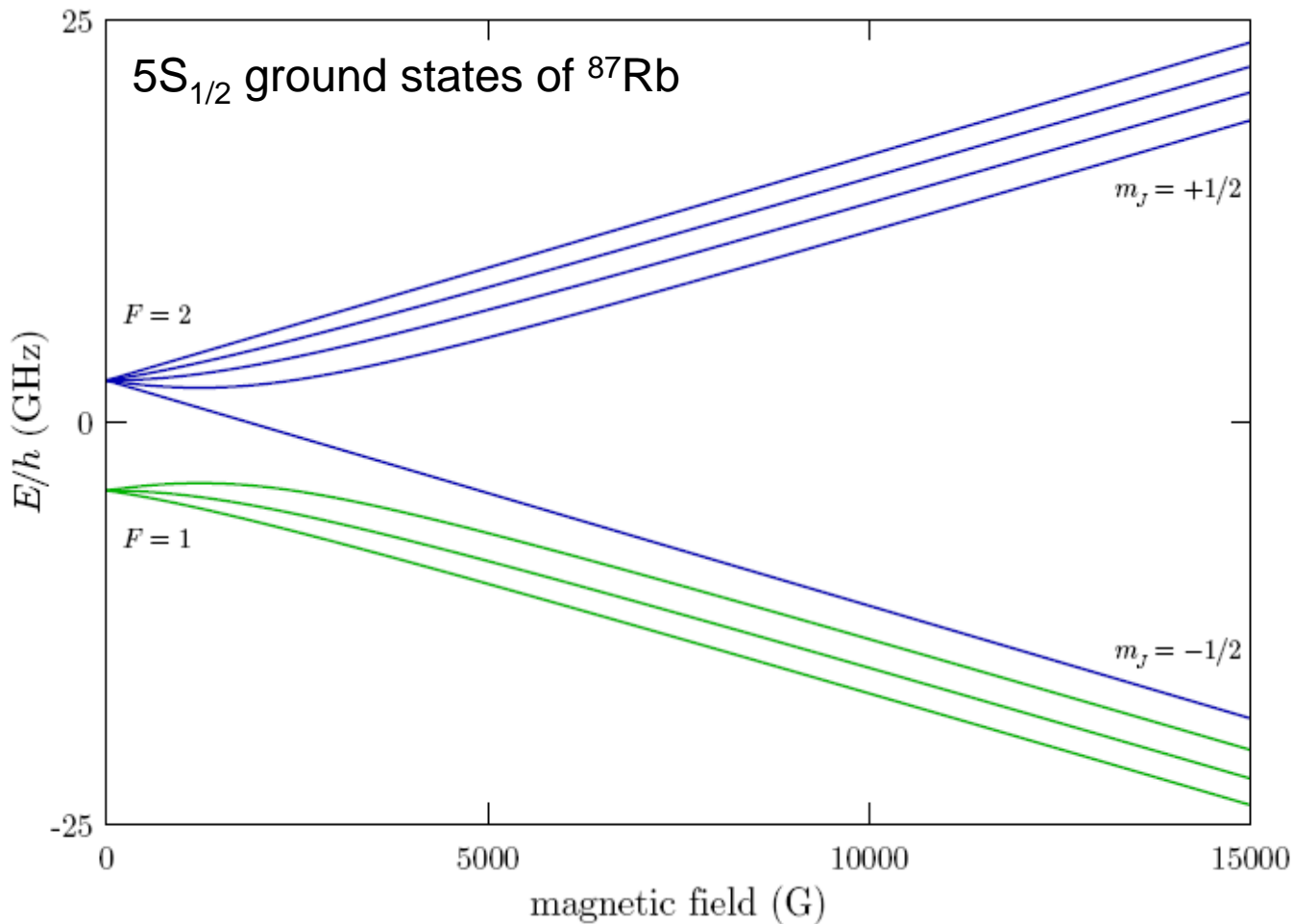


# Zeeman Sub-Structure

[  $^{87}\text{Rb}$ ,  $^{39}\text{K}$ ,  $^{41}\text{K}$  ]



# Zeeman Sub-Structure at High B-field



# Breit-Rabi Formula

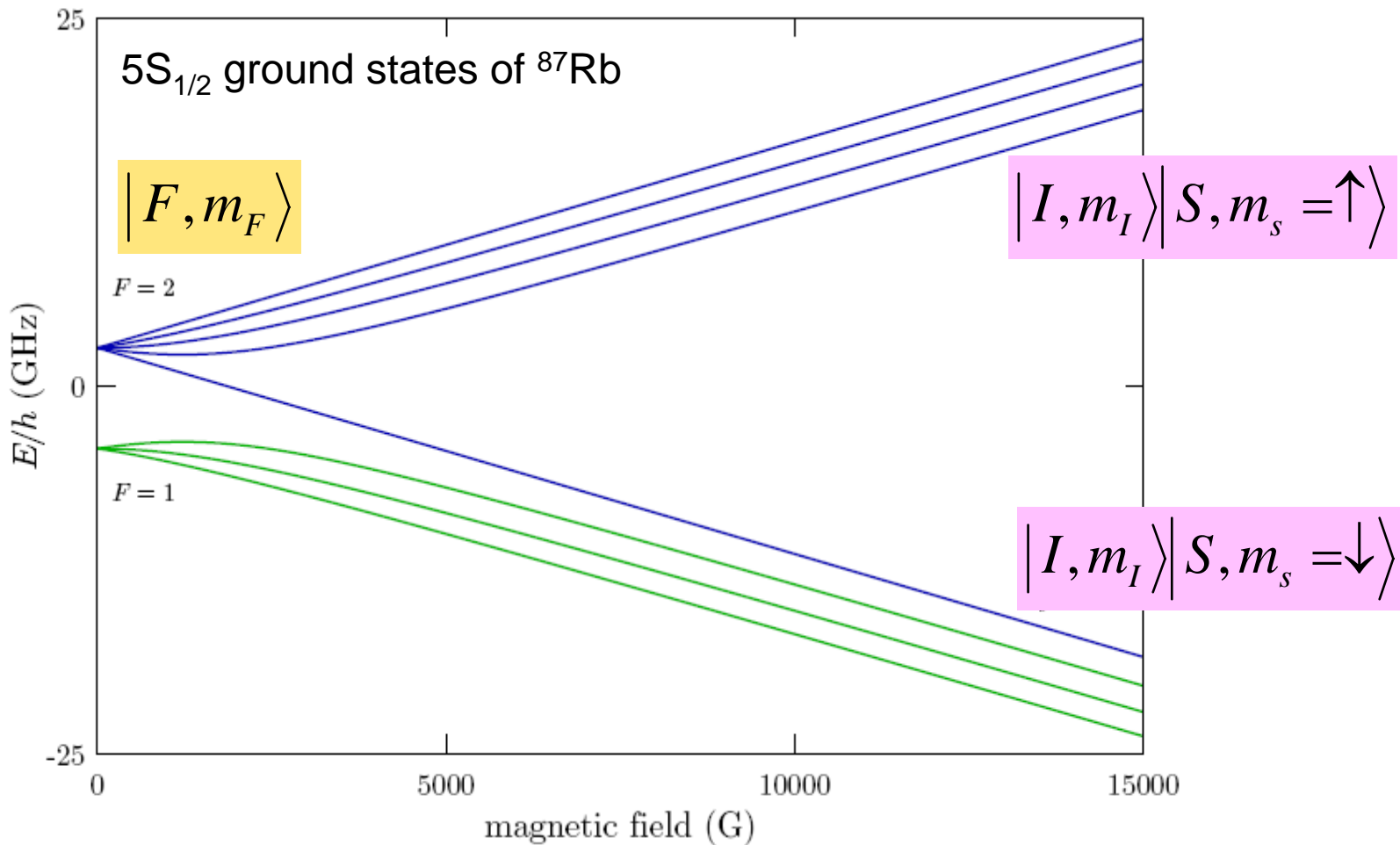
The Breit-Rabi formula for the Zeeman shift of atomic ground states is given by:

$$U(m_F, B) = g_I \mu_B m_F B + \frac{E_{hfs}}{2} \left( \pm \left( 1 + \frac{4m_F x}{2I + 1} + x^2 \right)^{1/2} - \frac{1}{2I + 1} \right),$$

where the  $\pm$  is used for the  $F = I \pm J$  state, respectively, and

$$x \equiv \frac{(g_J - g_I) \mu_B B}{E_{hfs}}.$$

# Zeeman Sub-Structure at High B-field



[Figure adapted from steck.us by Prof. Dan Steck, U. of Oregon (2010)]