

Pillars of Electrostatics

1. Inverse square law: Force $\propto 1/r^2$
2. Superposition principle

Inverse Square Law

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- Williams, Faller, and Hill (1971): $\varepsilon = (2.7 \pm 3.1) \times 10^{-16}$

Inverse Square Law vs. Quantum Electrodynamics

For $r \ll \lambda_{\text{Compton}}$ QED renormalizes the charge of the e^-

$$V(r) = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

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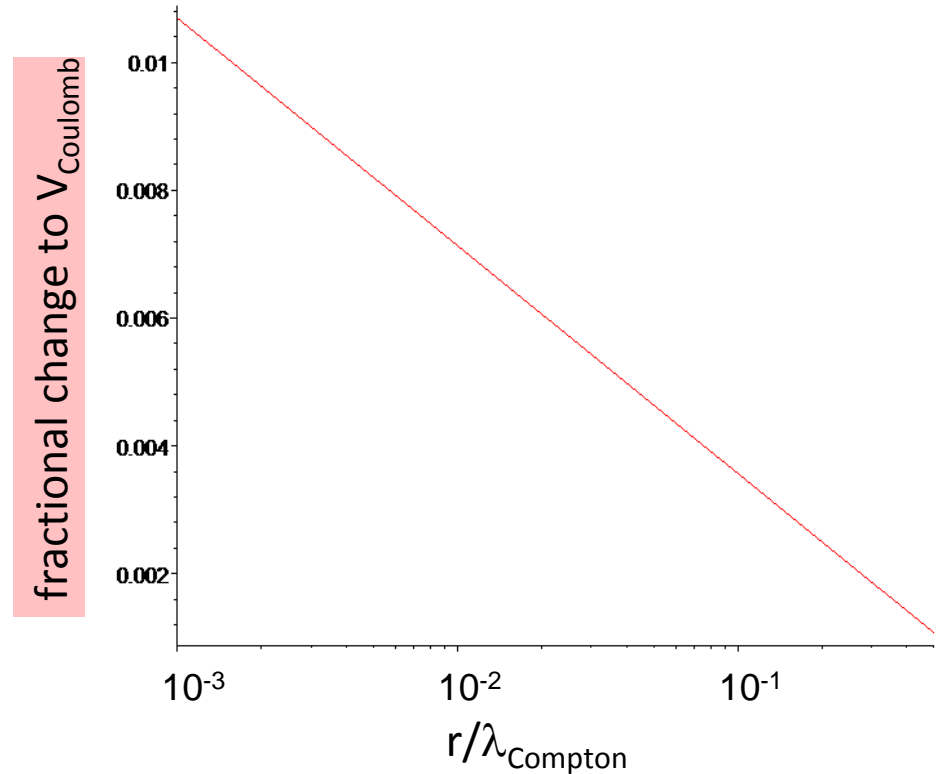
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Superposition Principle

In vacuum, the superposition principle ($\vec{E}_{total} = \vec{E}_1 + \vec{E}_2$) is true.

How true?

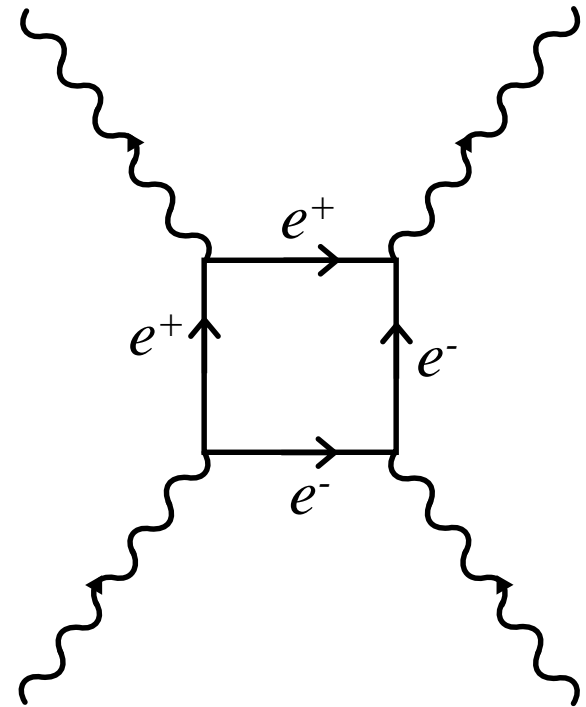
QED predicts that photons begin to interact with each other (vacuum polarization effect) for

$$\begin{aligned} E - \text{field} &\sim 10^{18} \text{ V/m} \\ B - \text{field} &\sim 10^9 \text{ T} \end{aligned}$$

Photon-photon scattering in vacuum has NOT been detected yet.

In non-linear optical media, photon-photon scattering is a common effect.

Note : $E_{max,LAB} \sim 10^{14} \text{ V/m}$ (ultrafast laser pulse)



Conclusion

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Both of these statements are true over the range of experimental conditions where one would use classical electrodynamics/electrostatics.