Today's Topics

Monday, September 10, 2025 (Week 3, lecture 8) – Chapter "end of 3", 4.6, 5.

0. Newton's version of Kepler's 3rd law.

1. Escape velocity

2. Tides

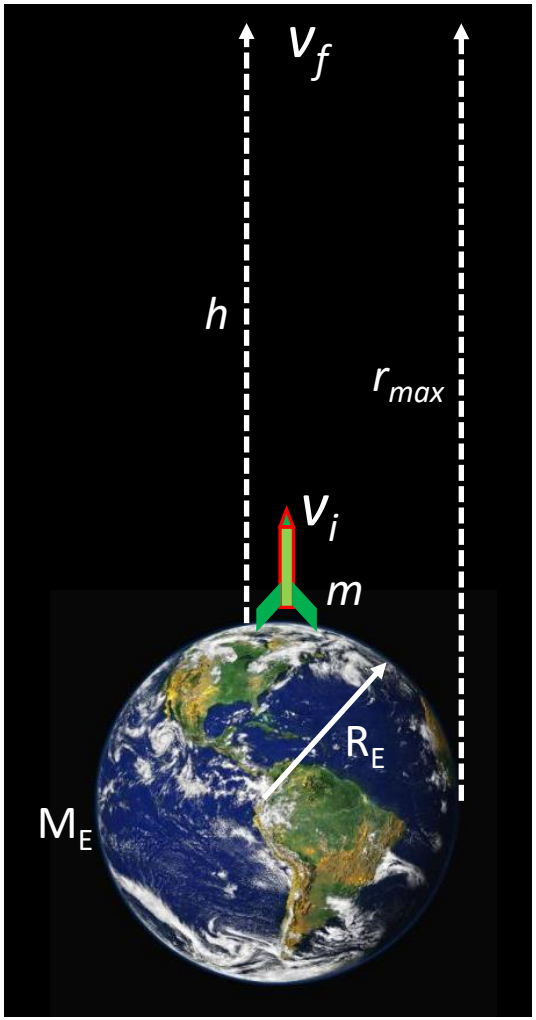
3. Electromagnetic waves

Reminder: Problem Set #3 is on ExpertTA and is due Friday, Feb. 14 by 9:00 am.

Escape Velocity

Question

What is the minimum velocity needed to escape Earth's gravity?



$$v_{escape} = \sqrt{\frac{2GM_E}{R_E}}$$

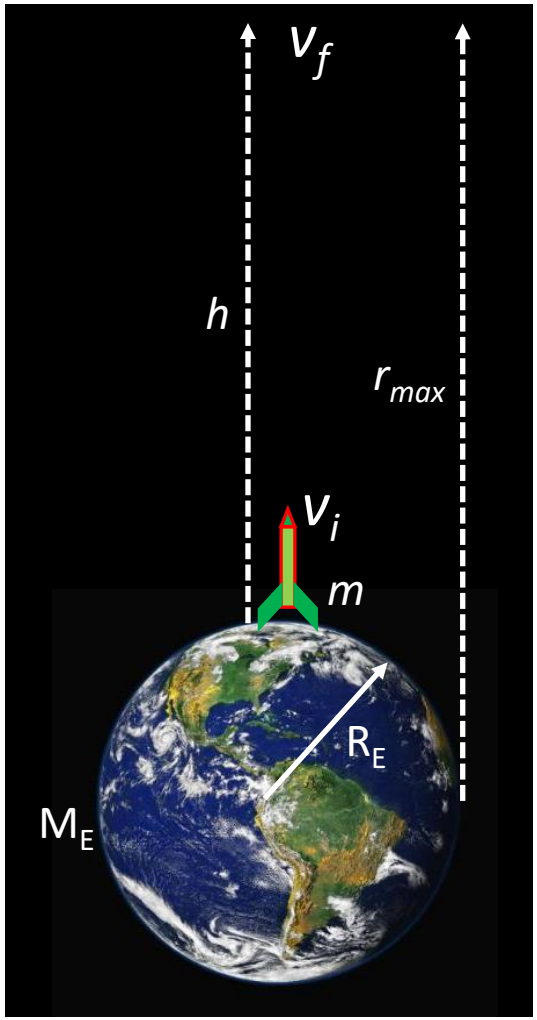
= 11.2 km/s on Earth

Note 1: escape velocity depends on your starting point.

Note 2: Since the Earth spins, objects at "rest" close to the equator already have a significant velocity.

→ Rockets are typically launched close to the equator (or in Florida)

Escape Velocity: Derivation



The projectile reaches its maximum altitude when

$$v_{final} = v_f = 0$$

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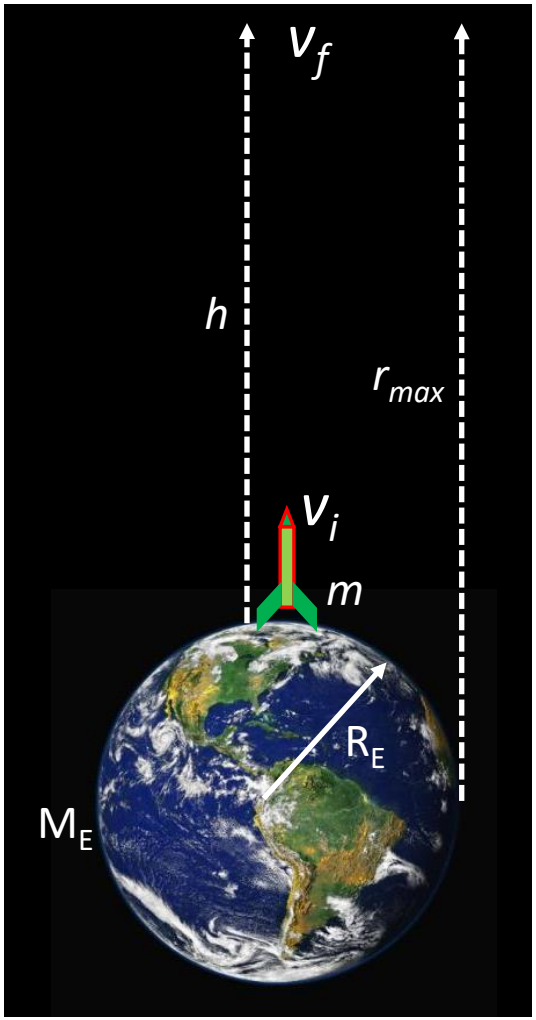

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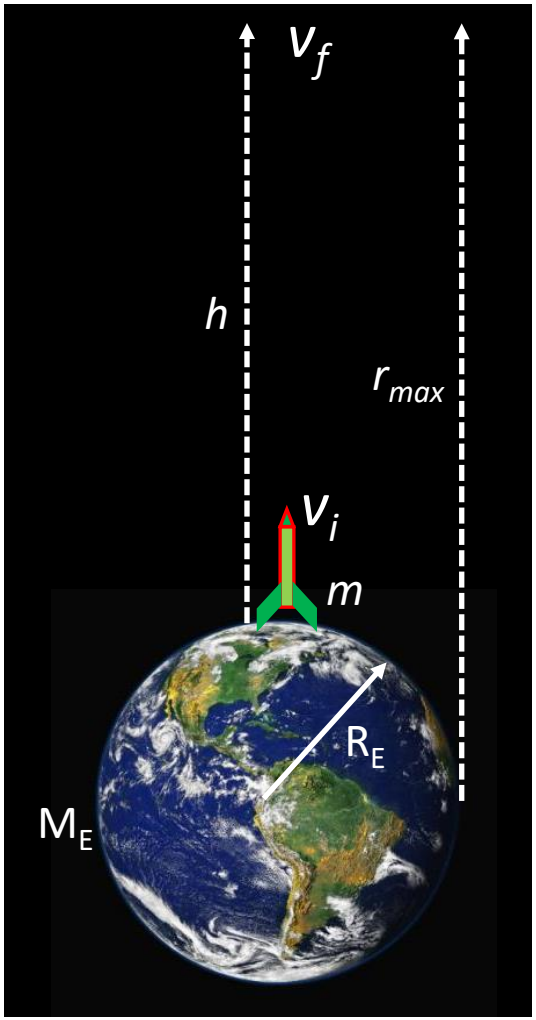

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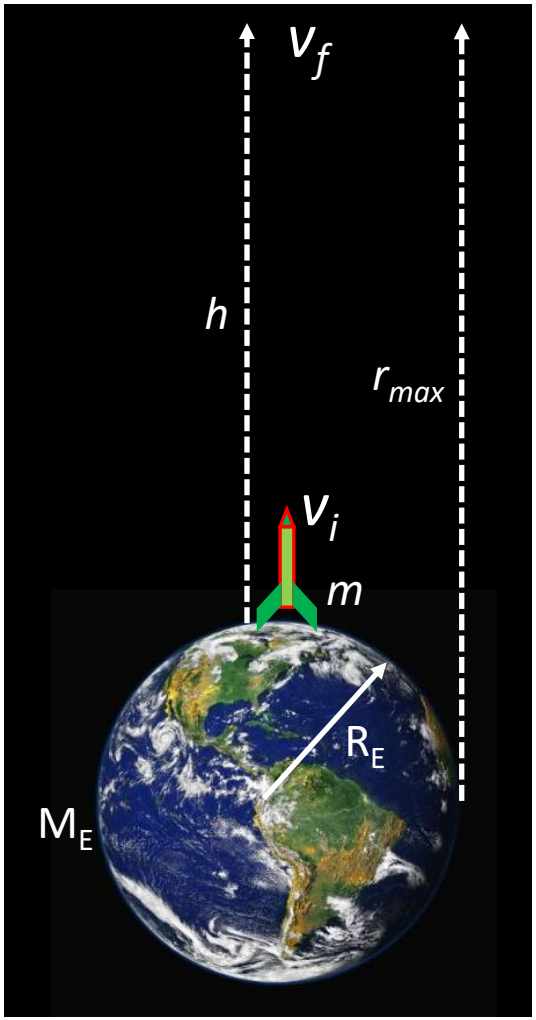

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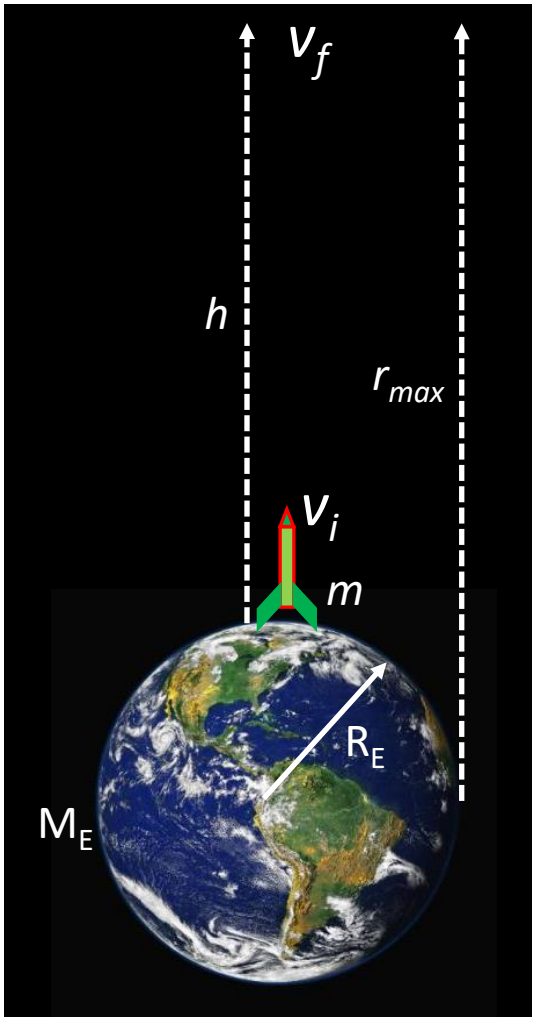

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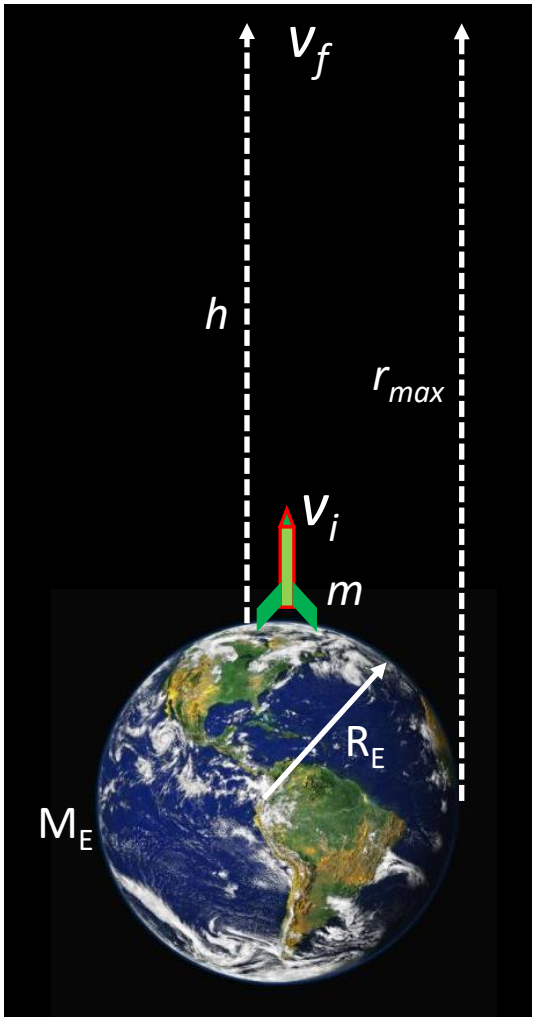

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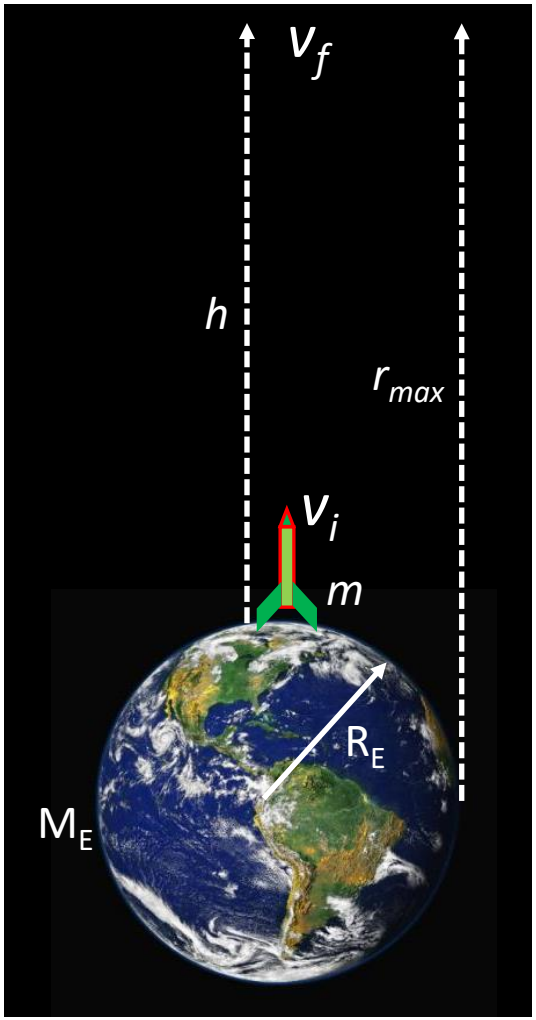

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$$v_{escape}^2 = 2GM_E\left(\frac{1}{R_E} - \frac{1}{r_{max\to\infty}}\right) \Rightarrow \boxed{v_{escape} = \sqrt{\frac{2GM_E}{R_E}}}$$

Tidal Force Example

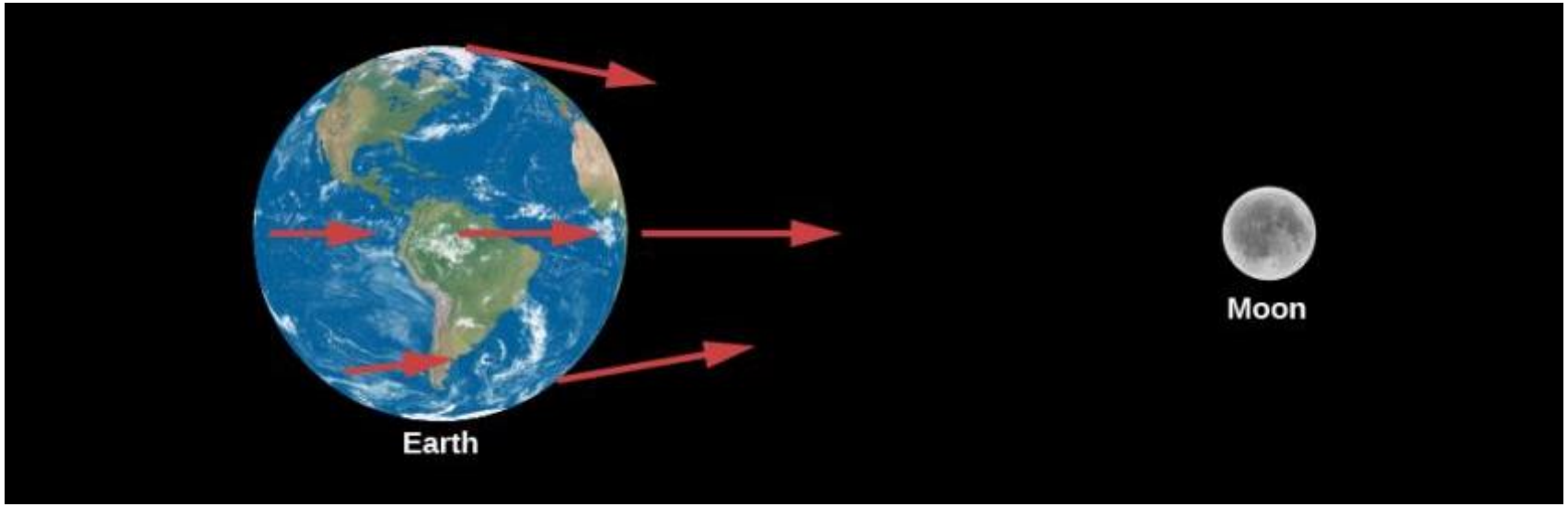
Ocean Tides

Ocean Tides

The force of **gravity** from the Moon is **not uniform** over the Earth.

→ gravity from Moon falls off as $1/r^2$.

→ Near face of Earth feels a stronger force than far face.



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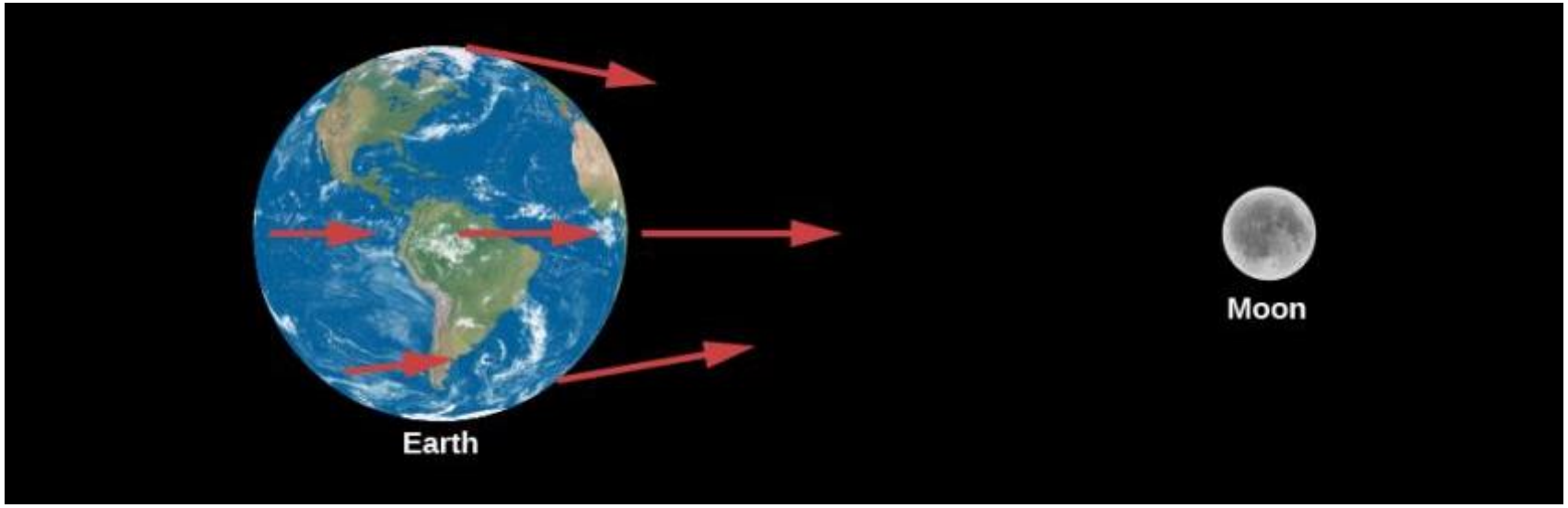


Result

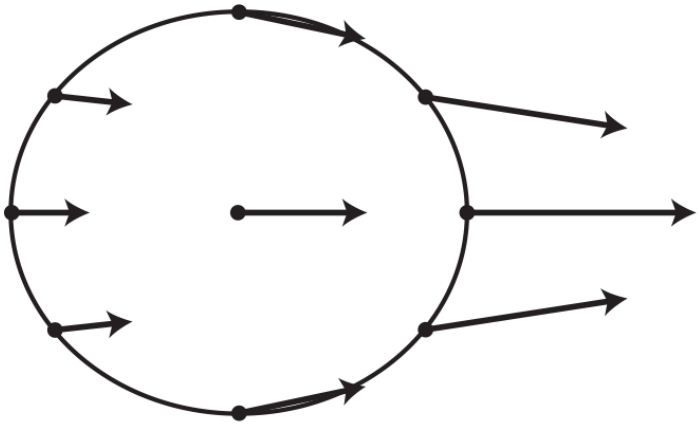
Water on **near side is pulled** towards Moon **more** than average Earth.

Water on **far side is pulled** towards Moon **less** than average Earth.

Ocean Tides: Effective Moon Gravity

Recall:

- Moon is in “free fall” orbit around Earth.
- Earth is in “free fall” orbit around Moon (albeit small orbit).



[scijinks.gov]

Moon

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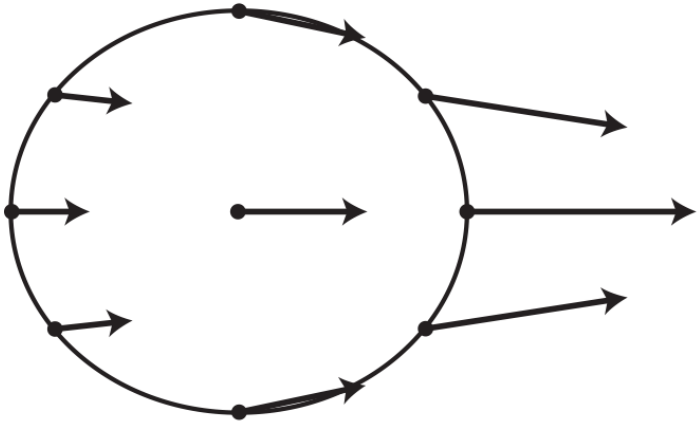
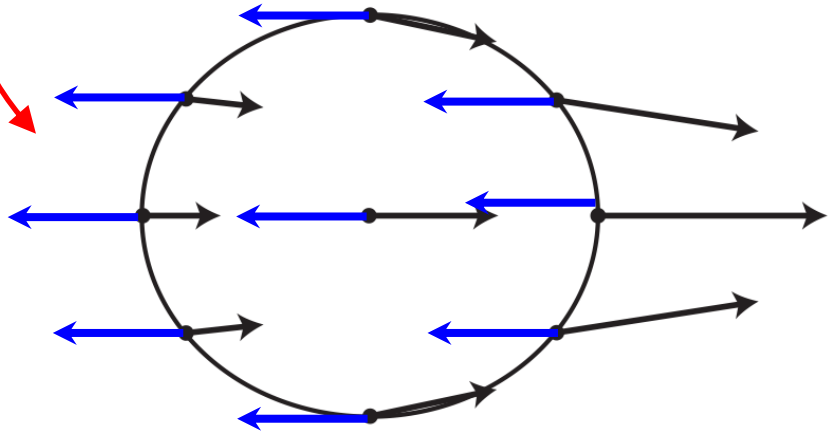


[scijinks.gov]

Moon

Subtract average gravitational force of Moon.

[since Earth is in “free fall” around Moon.]



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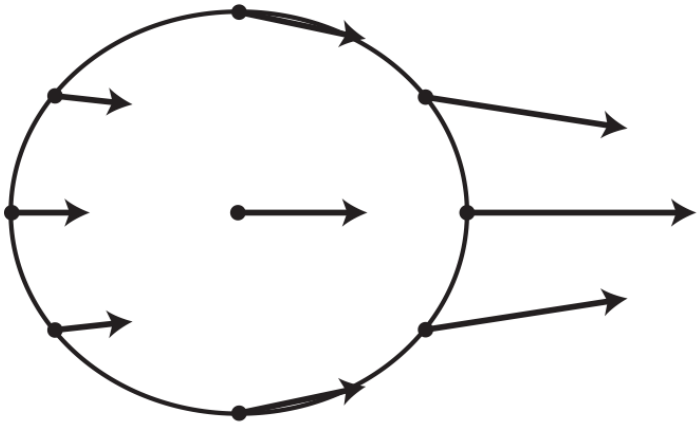

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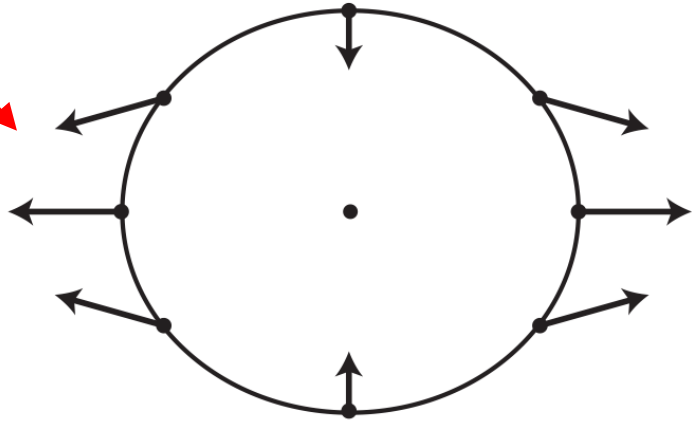

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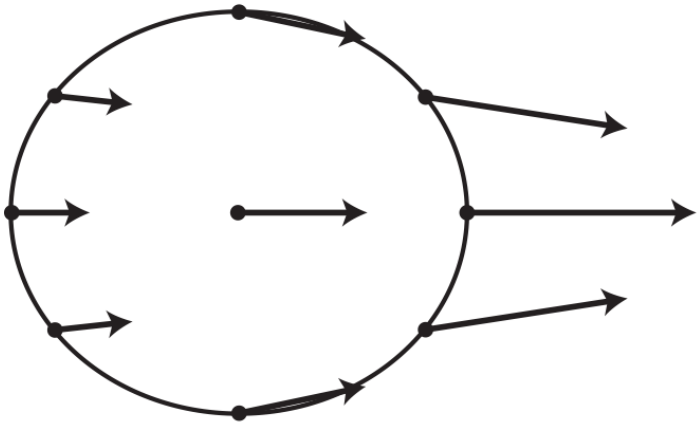
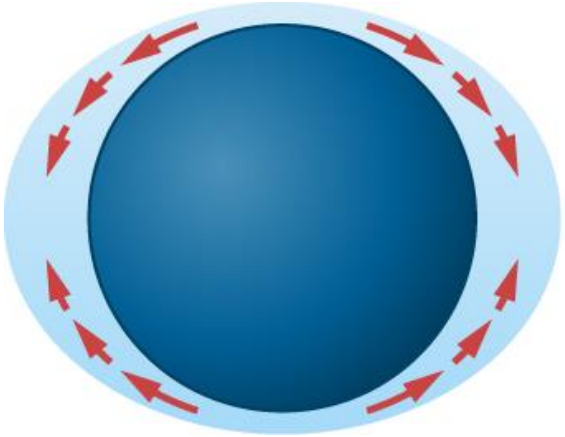


[scijinks.gov]

Moon

Ocean water is pulled by the effective force



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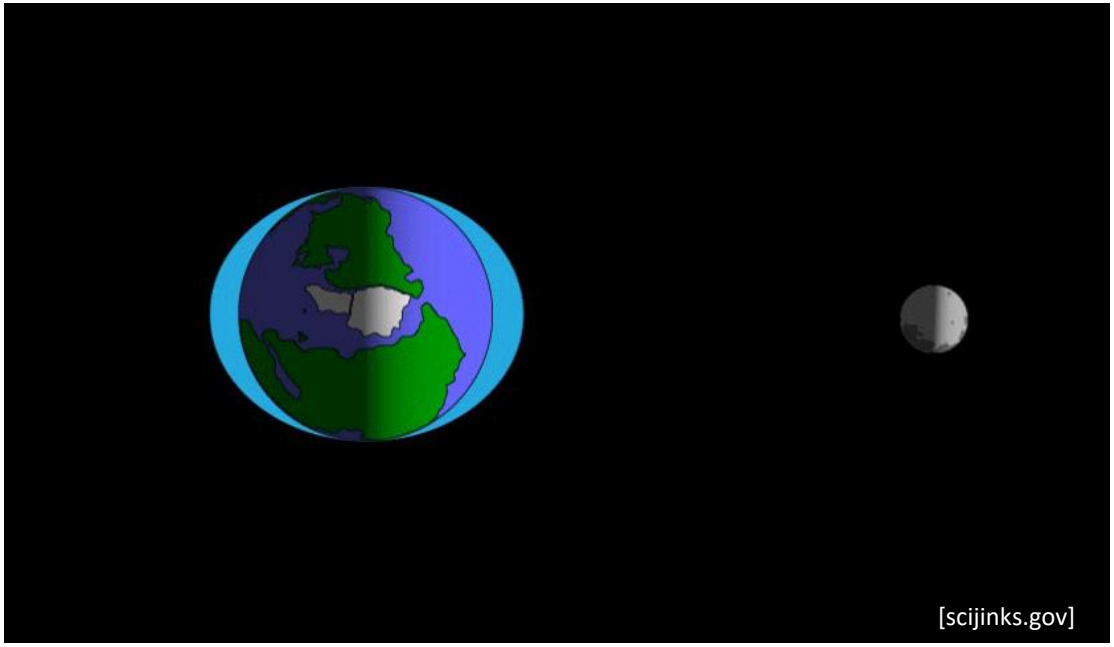

Animation of Earth and Oceans as seen from above North Pole.

Sun's gravity gradient affects tides as well: 46% of Moon's contribution.

- Tides are largest when Sun-Moon-Earth are aligned.
- Tides are weakest when Sun & Moon are at 90° to each other.
- Shape of ocean basins & winds also affect the strength of tides.
- The atmosphere also experiences tides.

PollEv Quiz: PollEv.com/sethaubin

Week 3
Light & Matter

1. Electromagnetic waves & photons

2. Spectroscopy and atoms

3. Particles, nuclei, and fusion

REMINDER: **Midterm #1** is on Friday, February 21 (in class).

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Speed of Light

The speed of light in **vacuum** is always $c = 3.0 \times 10^8$ m/s.

$= 300{,}000$ km/s

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The speed of light does NOT depend on the observer:

- **If observer A is at rest** and measures the speed of light of their laser pointer, then they will measure $\mathbf{c = 3.0 \times 10^8}$ **m/s**.
- **If observer B is moving at 290,000 km/s**, then they will measure the speed of light of observer A's laser pointer to be $\mathbf{c = 3.0 \times 10^8}$ **m/s**.

Speed of Light in Matter

The speed of light ***in matter is slower*** than in vacuum

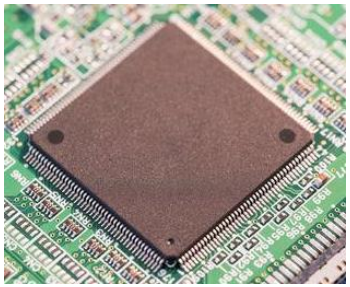
Speed of light in **air** **= 99.97% of c**

Speed of light in **water** **= 75% of c**

Speed of light in **glass** **= 67% of c**

Speed of light in **diamond = 41% of c**

Speed of light in **silicon** **≃ 25% of c**

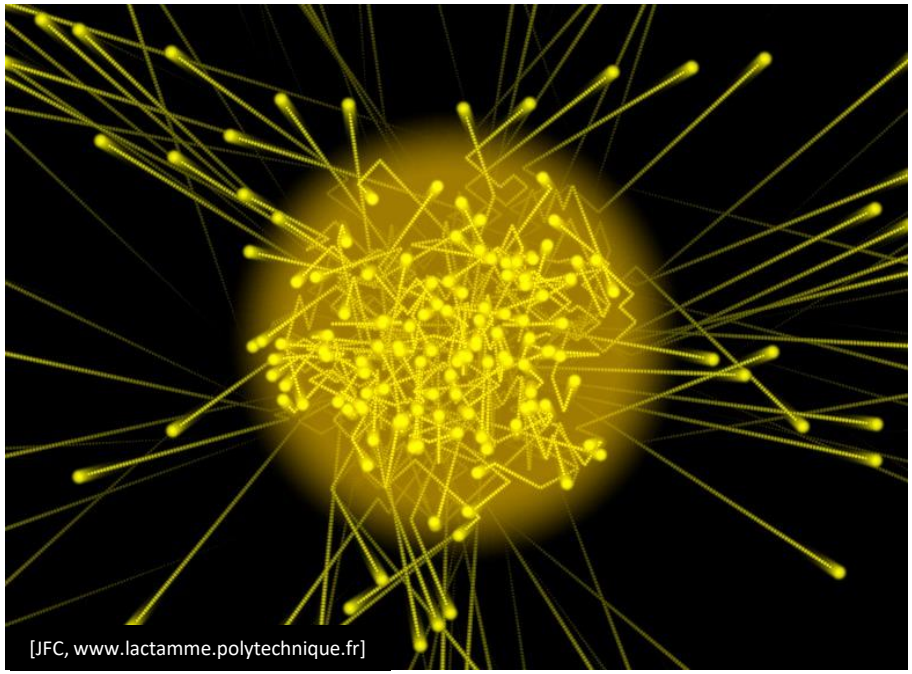


[123RF.com]

Note: In engineered atomic gases, light can be brought ~ 10 m/s and even stopped. (Novikova Lab at W&M)

Light:

Particle or Wave?



[JFC, www.lactamme.polytechnique.fr]

[Zachary Wilson, CK-12 Foundation, CC BY-NC 3.0]

Electromagnetic Waves

James Clerk Maxwell (1831-1879) worked on electricity and magnetism:

- They are different facets of the same phenomenon.
- Light is a wave of electric & magnetic fields.

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⬇

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[OpenStax]

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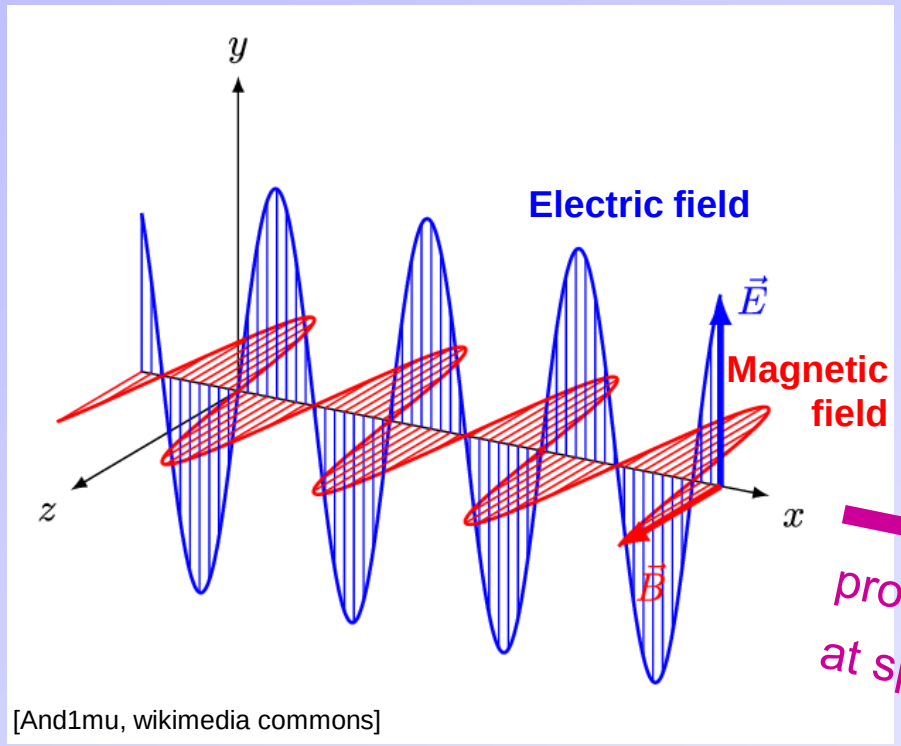

[And1mu, wikimedia commons]

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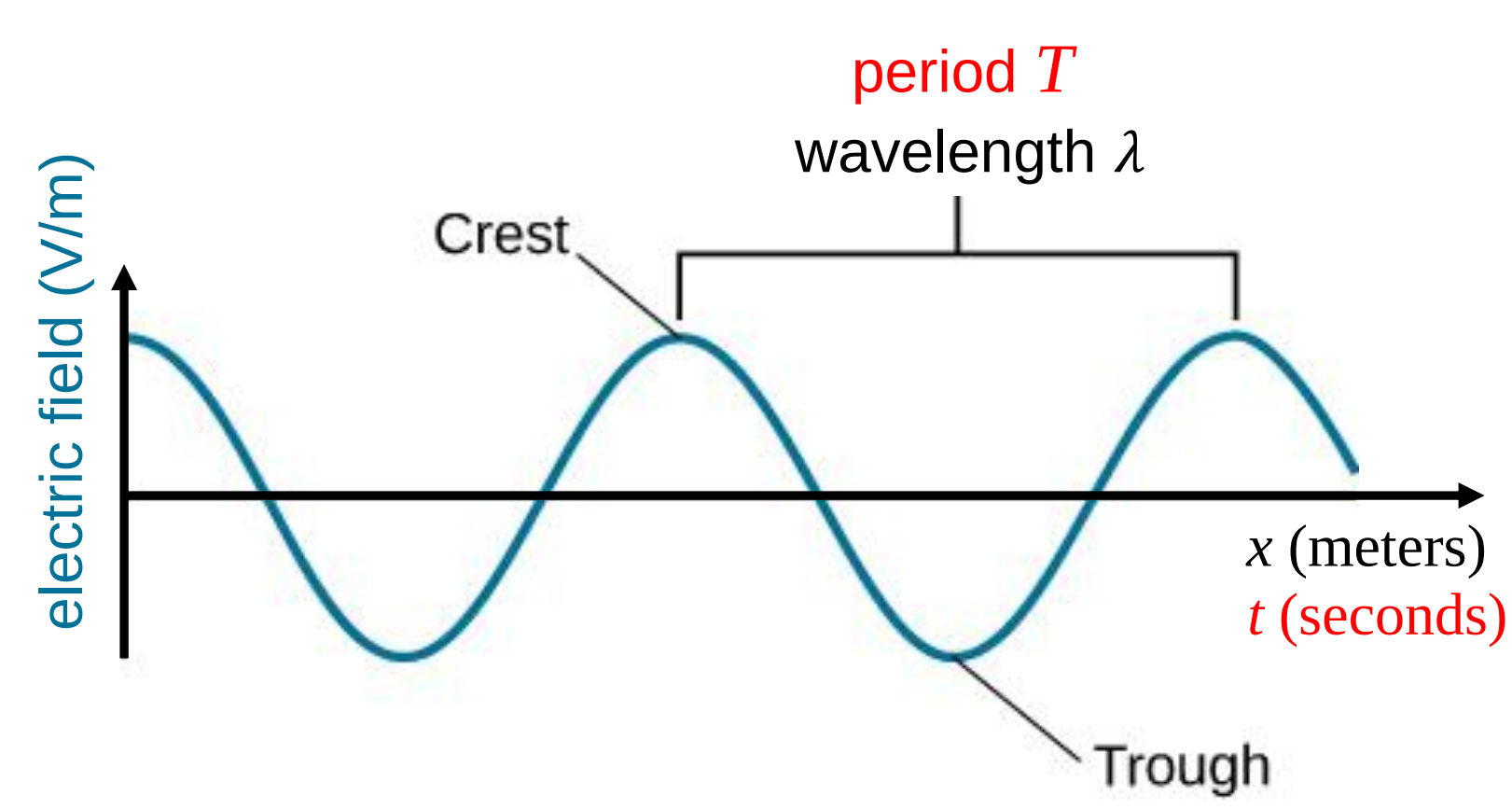
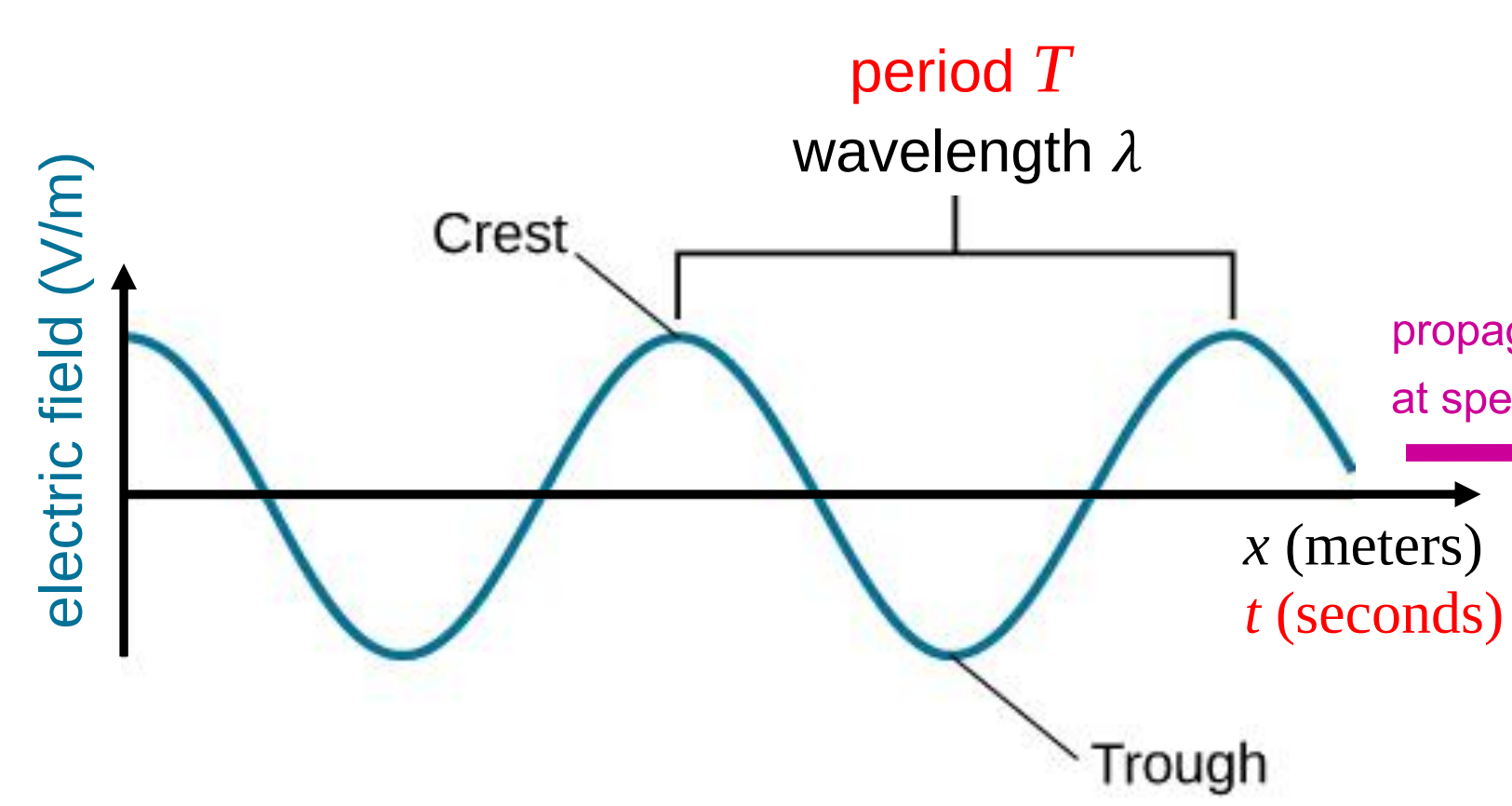
Wave Properties



Frequency: $f = \frac{1}{T}$ = oscillations per second

Wave Properties



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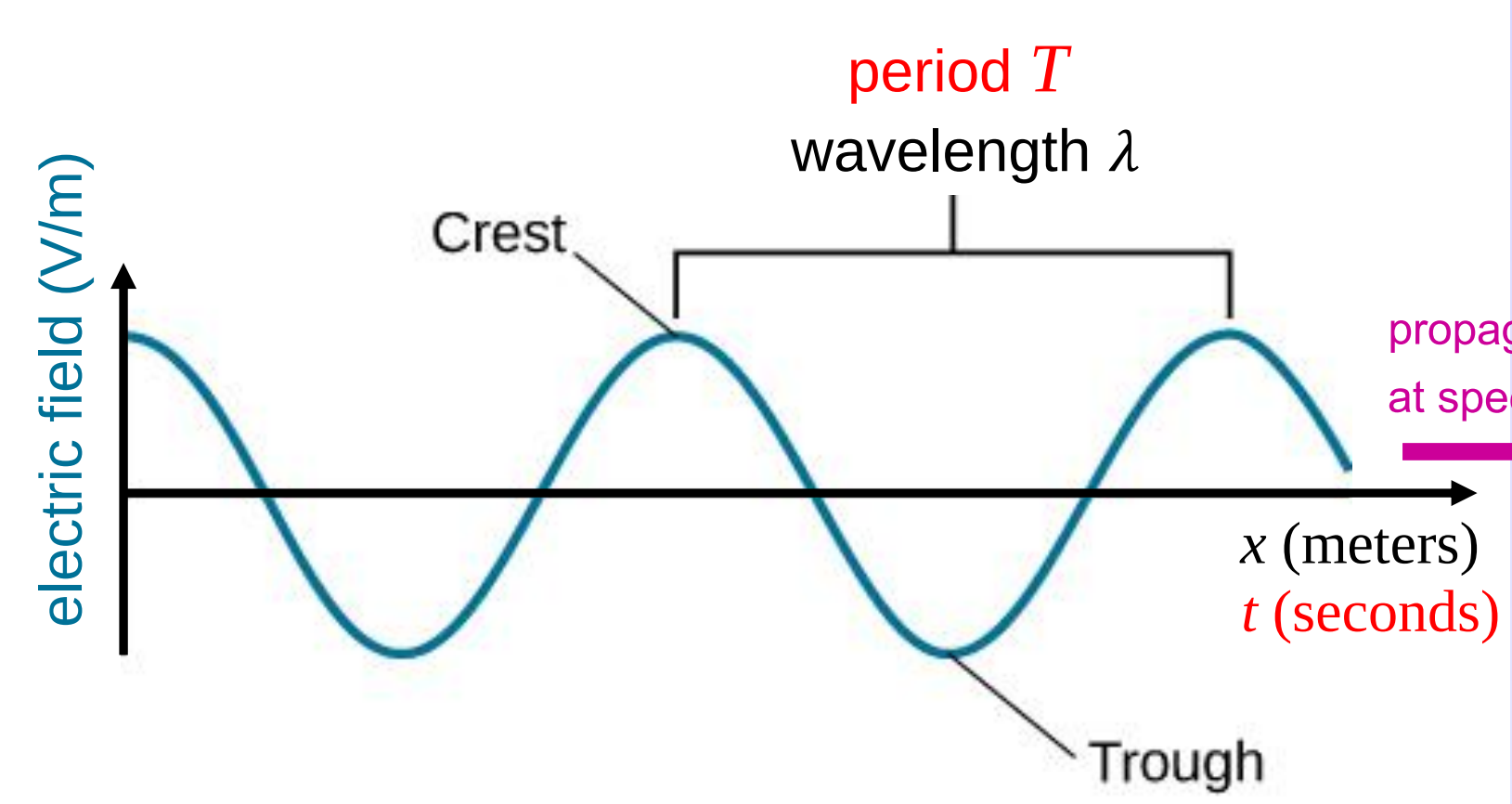

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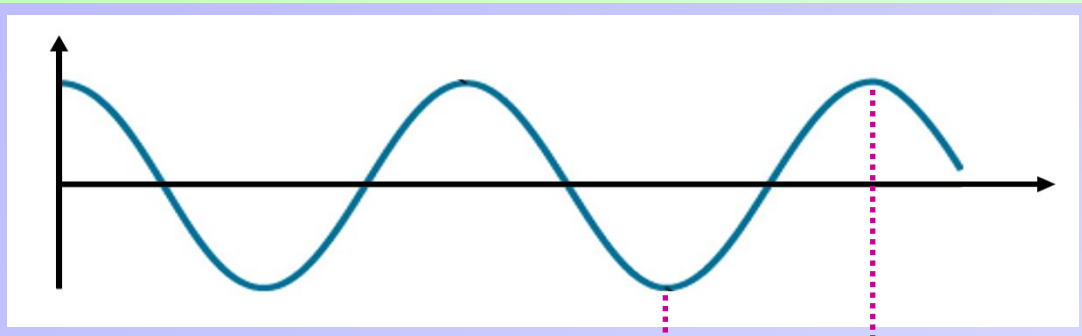
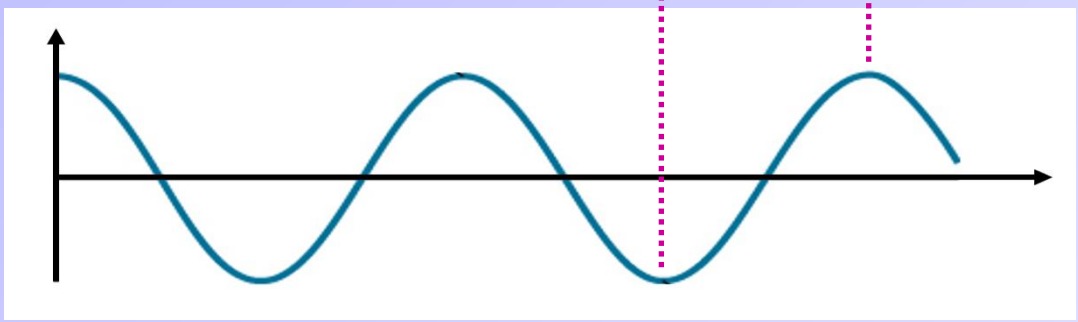
Traveling wave formula: $\lambda f = c$

Wave Addition: Constructive Interference



Troughs are in sync



Crests are in sync

+

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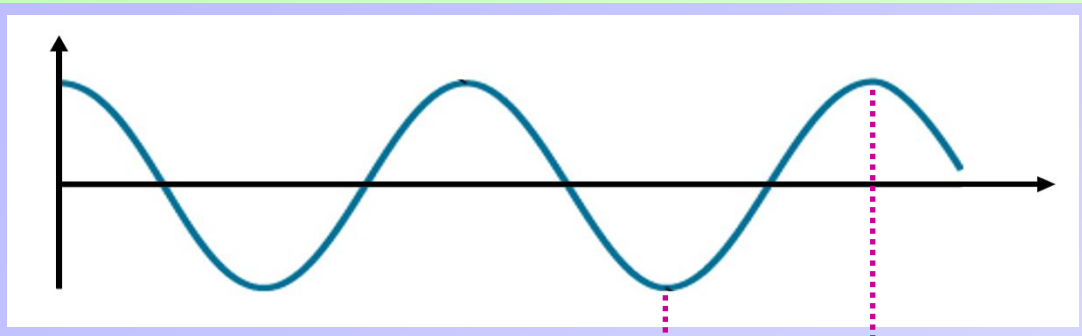

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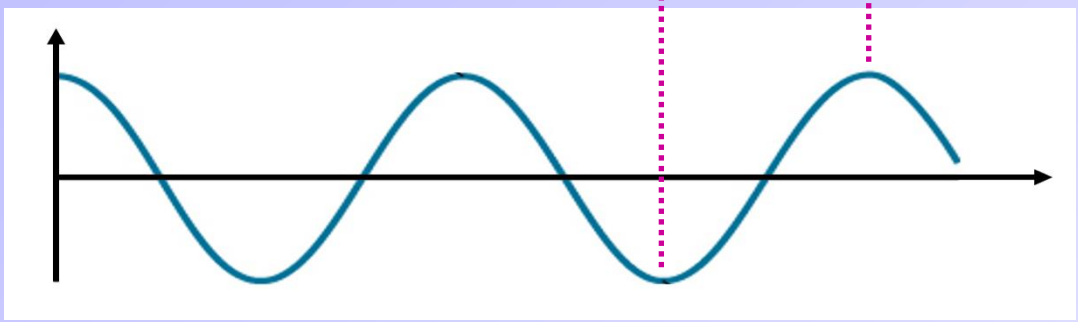

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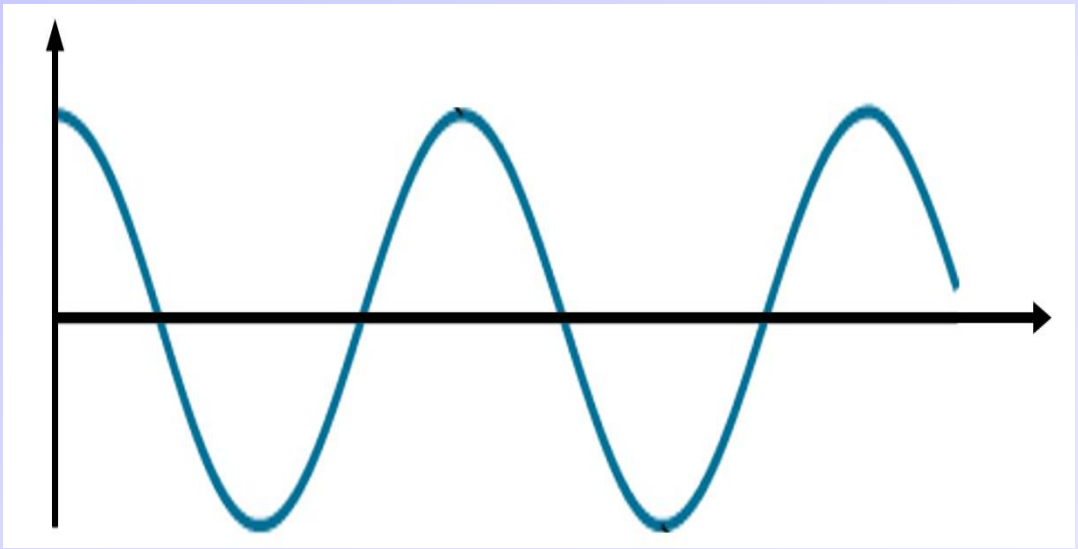
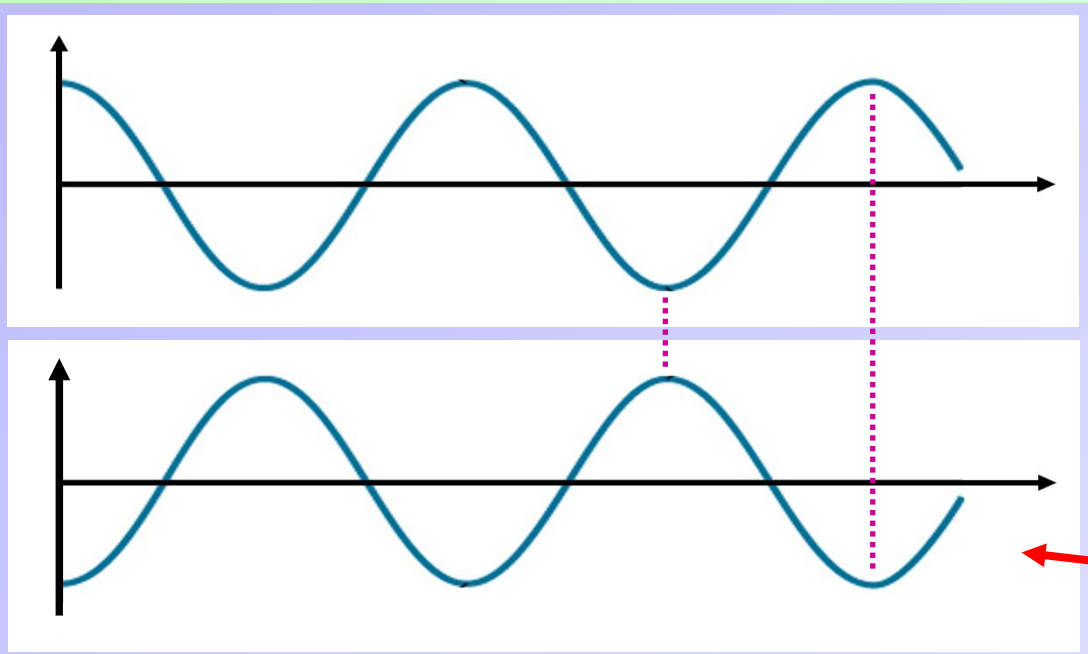


amplitude doubles

Wave Addition: Destructive Interference



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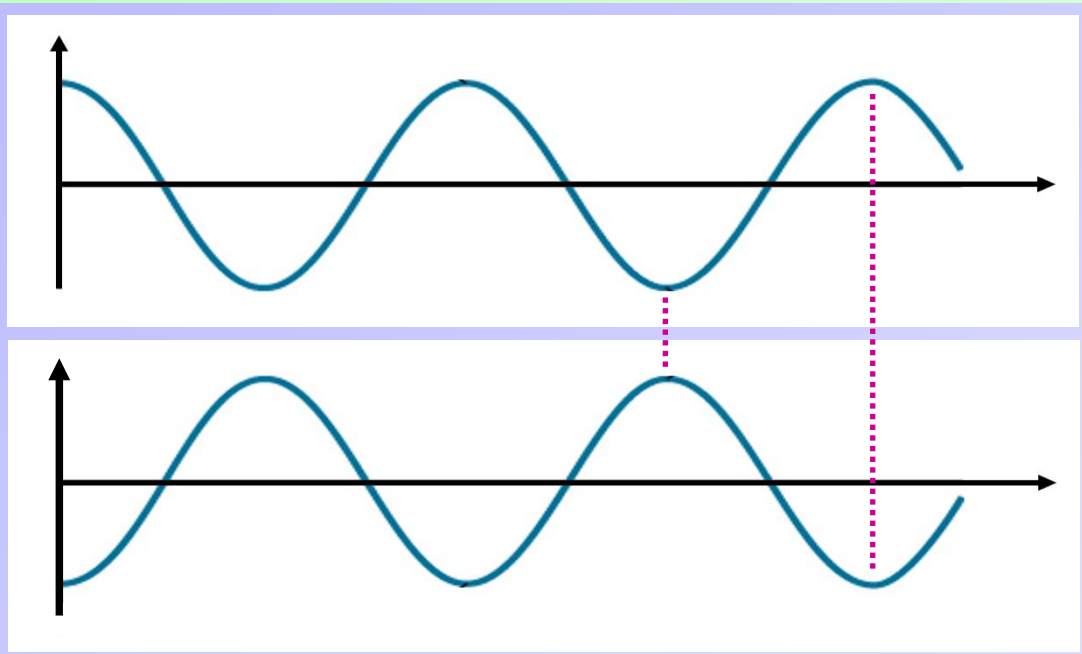
Troughs & crests are exactly out of sync

wave shifted by 180°

Wave Addition: Destructive Interference



+

Troughs & crests
are exactly
out of sync

amplitude
goes to <u>zero</u>
(wave disappears)