

## Formula Study Sheet

(i.e. formulas that you should know)

Gradient theorem

$$\int_{\text{path } P}^{\vec{r}_b} (\nabla f) \cdot d\vec{l} = f(\vec{r}_b) - f(\vec{r}_a)$$

Divergence Theorem

$$\int_V (\nabla \cdot \vec{F}) d^3r = \oint_{S(V)} \vec{F} \cdot d\vec{s}$$

Stokes's Theorem

$$\int_S (\nabla \times \vec{F}) \cdot d\vec{s} = \oint_{C(S)} \vec{F} \cdot d\vec{\ell}$$

Divergence of  $1/r^2$  - point source

$$\vec{\nabla} \cdot \frac{\hat{r}}{r^2} = 4\pi\delta^3(\vec{r}) \quad \& \quad \nabla^2 \frac{1}{r} = -4\pi\delta^3(\vec{r})$$

Coulomb's law

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{12}^2}$$

Electric field of a point charge  $q$  at  $\vec{r}'$

$$\vec{E}_q = \frac{1}{4\pi\epsilon_0} \frac{q}{|\vec{r} - \vec{r}'|^2} (\widehat{r - r'})$$

Electric field of a charge distribution  $\rho(\vec{r}')$

$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho(\vec{r}')}{|\vec{r} - \vec{r}'|^2} (\widehat{r - r'}) d^3r'$$

Potential of a point charge  $q$  at  $\vec{r}'$

$$V_q(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{|\vec{r} - \vec{r}'|}$$

Potential of a charge distribution  $\rho(\vec{r}')$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho(\vec{r}')}{|\vec{r} - \vec{r}'|} d^3r'$$

Electric field and potential

$$\vec{E} = -\vec{\nabla}V \quad \& \quad V(\vec{r}) = -\int_{\vec{r}_0}^{\vec{r}} \vec{E} \cdot d\vec{\ell}$$

Electric field of a plane of charge

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{n}$$

Electric field across a plane of charge

$$\Delta E_{\perp} = \frac{\sigma}{\epsilon_0} \quad \& \quad \Delta E_{\parallel} = 0$$

Gauss's law

$$\vec{\nabla} \cdot \vec{E} = \frac{\rho(\vec{r})}{\epsilon_0} \quad \& \quad \oint_S \vec{E} \cdot d\vec{s} = \frac{q_{\text{enclosed}}}{\epsilon_0}$$

Electrostatic field has no curl

$$\vec{\nabla} \times \vec{E} = 0$$

Laplace's equation

$$\nabla^2 V(\vec{r}) = 0$$

Poisson's equation

$$\nabla^2 V(\vec{r}) = \frac{\rho(\vec{r})}{\epsilon_0}$$

Electrostatic energy

$$U_E = \frac{\epsilon_0}{2} \int \vec{E}^2 d^3r$$

Capacitor of capacitance  $C$

$$C = \frac{Q}{V} \quad \& \quad U_E = \frac{1}{2} CV^2$$