

PHYS 404 and 690-03

Problem set due Friday, April 29, 2011.

The Quantized Electromagnetic Field

1. Coherent States I

Consider two coherent states $|\alpha\rangle$ and $|\beta\rangle$. Show that they are not orthogonal by proving the relation:

$$\langle\alpha|\beta\rangle = \exp\left[-\frac{1}{2}\left(|\alpha|^2 + |\beta|^2 - 2\alpha^*\beta\right)\right]$$

(Meystre and Sargent, problem 13.2)

3. Coherent States II

For a coherent state $|\alpha\rangle$ with $\alpha=10$ calculate:

- the mean photon number.
- the fluctuations or variance of the photon number.
- the quantum uncertainty in the optical phase.

2. Vacuum fluctuations

Calculate the variance of the electric field in the vacuum state for a given wavevector and polarization. Write $(\hat{a}\hat{a}^\dagger)^3$ in normal order.

(Meystre and Sargent, problem 13.6)

4. Casimir Force

Calculate the Casimir force in Newtons between two conducting plates of area 1 cm^2 each separated by a) 1 mm and b) $1\text{ }\mu\text{m}$. Compare the force to the strength of gravity on Earth.